

Surname	Centre Number	Candidate Number
First name(s)		2



GCE A LEVEL

1305U60-1



S24-1305U60-1

WEDNESDAY, 12 JUNE 2024 – AFTERNOON

FURTHER MATHEMATICS – A2 unit 6
FURTHER MECHANICS B

1 hour 45 minutes

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1	11	
2	16	
3	13	
4	13	
5	13	
6	14	
Total	80	

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a Formula Booklet;
- a calculator.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** questions.

Take g as 9.8 ms^{-2} .

Write your answers in the spaces provided in this booklet. If you run out of space, use the additional page(s) at the back of the booklet, taking care to number the question(s) correctly.

INFORMATION FOR CANDIDATES

The maximum mark for this paper is 80.

The number of marks is given in brackets at the end of each question or part-question.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Answers without working may not gain full credit.

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

You are reminded of the necessity for good English and orderly presentation in your answers.



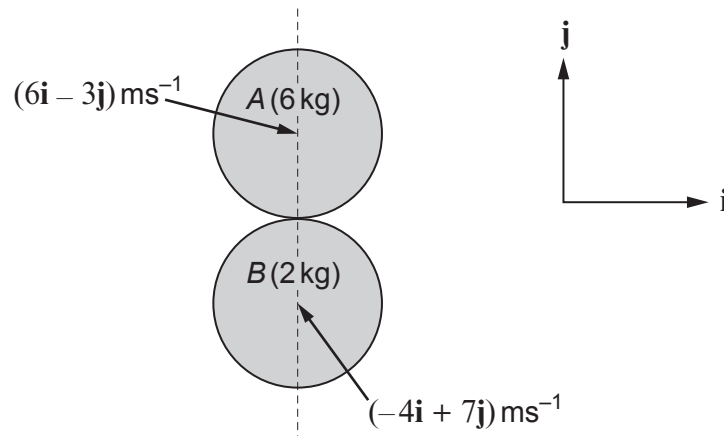
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Reminder: Sufficient working must be shown to demonstrate the **mathematical** method employed.

1. Two smooth spheres A and B are moving on a smooth horizontal plane when they collide obliquely. When the spheres collide, the line joining their centres is parallel to the vector \mathbf{j} , as shown in the diagram below.

Immediately before the collision, sphere A has velocity $(6\mathbf{i} - 3\mathbf{j})\text{ ms}^{-1}$ and sphere B has velocity $(-4\mathbf{i} + 7\mathbf{j})\text{ ms}^{-1}$. Sphere A has mass 6 kg and sphere B has mass 2 kg .



Immediately after the collision, sphere B has velocity $(-4\mathbf{i} - 5\mathbf{j}) \text{ ms}^{-1}$.

- (a) Find the velocity of A immediately after the collision.

[3]



- (b) Calculate the coefficient of restitution between A and B .

[3]

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- (c) Find the angle through which the direction of motion of B is deflected as a result of the collision. Give your answer correct to the nearest degree.

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- (d) After the collision, sphere B continues to move with velocity $(-4\mathbf{i} - 5\mathbf{j})\text{ms}^{-1}$ until it collides with another sphere C , which exerts an impulse of $(-20\mathbf{i} + 18\mathbf{j})\text{Ns}$ on B .

Find the velocity of B after the collision with C .

[2]

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(b) Calculate the time taken for the object to hit the ground.

[6]

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- (c) Given that the distance of the object from A at time t is x metres, form another differential equation to find an expression for x in terms of v . Hence, find the height of A above the ground. [7]

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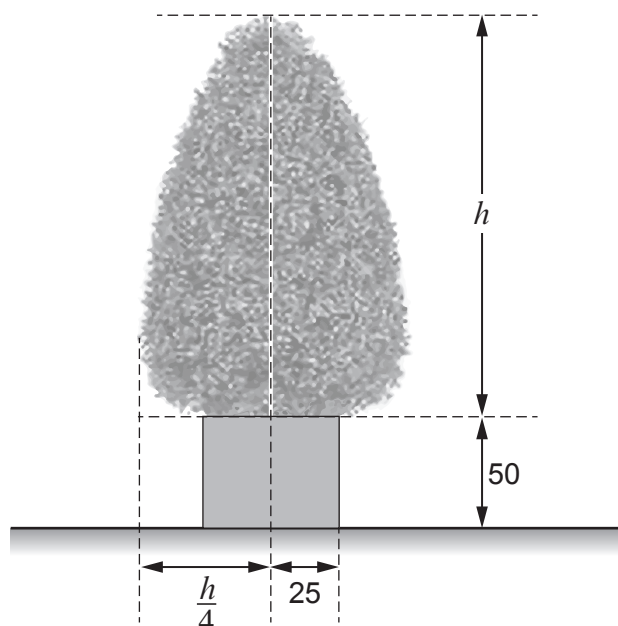
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The diagram below shows a small tree growing in a pot. The uniform solid S described on the previous page may be used to model the part of the tree above the pot. This part of the tree has height h cm and base radius $\frac{h}{4}$ cm. The pot, including its contents, may be modelled as a solid cylinder of height 50 cm and radius 25 cm.



You may assume that the density of the pot, including its contents, is equal to 20 times the density of the part of the tree above the pot.



- (b) A gardener suggests that a tree is said to have outgrown its pot if the centre of mass, of both the tree and its pot, lies above the height of the pot. Determine the maximum value of h before the tree outgrows its pot. [8]

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- (c) Identify one possible limitation of the model used that could affect your answer to part (b).

[1]

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END OF PAPER



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